Friday Sept 17, 2021 Math Notes (Calculus III) Note: Good Notes wasn't an option today; The iPad is out of battery!!! no Ex: Compute the tangent line for at (J3, 1, 2) r(t)=12cos(t), 2sin(t), 4cos(2t)> RetCon Comment : The limit lim to is not indeterminate,

50 L'Hapital does not apply Next Week: Monday: Normal Lecture wednesday: review for exam + bring Questions (Inclass) Friday: Exam 01 So... Study !! look over EVERTHING!! (Watch lectures and do practice) Back to the example (above) Sol: (t) = <-2sin(t), 2cos(t), -8sin(t)> Infinite possibilities $\sqrt{3} = 2\cos(4)$ (cos(tt) = $\frac{3}{2}$ $1 = 2\sin(4)$ \rightarrow (sin (t) = $\frac{1}{2}$ $2 = 4\cos(2t)$ (cos(2t) = $\frac{1}{2}$ >t= 1/4 2km Check: $\cos\left(2\cdot\frac{\pi}{6}\right) = \cos\left(\frac{\pi}{3}\right) = \frac{1}{2}\sqrt{$.. The tangent vector at the given point is: $F(\sqrt[\pi]{6}) = \langle -2\sin(\frac{\pi}{6}), 2\cos(\frac{\pi}{6}), -8\sin(2\cdot\frac{\pi}{6}) \rangle$ =<-1, 13, -413>

.. the tangent line has a vector equation: P+t7(7)

JY= = |X|

Arclength =
$$\int_{t=a}^{s} \sqrt{\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2} dt$$

Ex: Find the arc length of
$$\overrightarrow{r}(t) = \angle \cos(t)$$
, $\sin(t)$, $\ln(\cos(t)) >$ on $0 \le t \le 10$

$$a = 0$$
 $b = \frac{\pi}{4}$ $r'(t) = \langle -Sin(t), cos(t), \frac{-Sin(t)}{cos(t)} \rangle$

$$|r'(t)| = \sqrt{(sin(t))^2 + (cos(t))^2 + (-tan(t))^2}$$

Problem Continued

$$6 = \pi$$
 $\alpha = \frac{\pi}{3}$ $r'(t) = \langle -\sin(t), \cos(t), 2t \rangle$

$$S = \int_{1+4t^{2}}^{\pi} dt = \int_{\frac{1}{2}}^{\pi} \sqrt{1+4t^{2}} 2dt$$

$$t = \frac{\pi}{3}$$



-tand = 2t

J1+4+ = Jec(0)

